

## SCHWARZSCHILD RADIUS

This can be obtained by equating the Newtonian escape speed  $v_N$  to the speed of light  $c$ . To obtain  $v_N$  set the initial kinetic energy  $KE = \frac{1}{2}mv_N^2$  of a mass  $m$  equal to the change in potential energy  $PE = GMm/R_s$  in going from a distance  $R_s$  (the Schwarzschild radius) to an infinite distance away from a mass  $M$  :

$$\frac{1}{2}mv_N^2 = \frac{1}{2}mc^2 = GMm/R_s \Rightarrow R_s = 2GM / c^2. \quad (1)$$

The term  $\frac{1}{2}mc^2$  does not look relativistic and it is not, but  $mc^2$  cannot be used because the change in potential energy  $GMm/R_s$  on the right hand side of eq. (1) is not relativistic. Equation (1) is the same as the general relativity (GR) result.

The Schwarzschild radius for a Planck mass  $m_p = (hc / G)^{1/2}$  is  $R_s = (2Gm_p / c^2)$   
 $= 2(hG / c^3)^{1/2}$ , twice the Planck length.